

Max Square Roots

What is a Square?

- a) A figure with four equal right-angled sides whose Area = side \times side.
- b) A number or variable raised to the 2^{nd} power, like 3^2 or x^2 .
- c) The result of multiplying a number by itself: 9 is the square of 3×3 .
- d) All of the above.

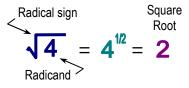
Answer: d

Area 2×2 Square 2

What is a Square Root?

- a) A number multiplied by itself to produce a square, like $2 \times 2 = 4$.
- b) A number or variable raised to the $\frac{1}{2}$ power, like $9^{1/2}$ or $x^{1/2}$.
- c) The result of taking the square root of a number; 3 is the root of $\sqrt{9}$.
- d) All of the above.

Answer: d



Perfect Squares

Extracting A Square Root

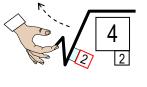


Imagine you have a square tooth with two identical roots. One root is inflamed, so you go to the dentist who removes it with a Root Extraction Tool.



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Square Tooth	Extraction Tool	
4 2 2	4 2 2	<
Inflamed Root	Dental Glue	



2 Extracted Root

Perfect Squares

Teeth that are perfectly square have *integer* roots.

Integers consist of whole numbers and their negatives: ...-2, -1, 0, 1, 2....

Teeth can also have negative square roots since $- \times - = +$.

Example: $-3 \times -3 = 9$, so -3 is a square root of 9. $\pm \sqrt{9} = \pm 3$

Non-Perfect Squares

Teeth that are *not* perfectly square have *irrational* roots.

Irrational numbers never end and never repeat their digit patterns.

Example: $\sqrt{2} = 1.4142135...$

To Estimate Roots of Non-Perfect Squares

Fit the non-perfect square between perfect squares. Try roots in between. Problem: Estimate the square root of 20 to one decimal place.

Procedure: In the **Perfect Squares** table, 20 fits about halfway between squares 16 and 25, so its square root should be about halfway between their roots of 4 and 5.

Trials: $4.4 \times 4.4 = 19.36$ $(4.5 \times 4.5 = 20.25)$ $4.6 \times 4.6 = 21.16$

Closest Root: 4.5

Periect Squares		
Root	Square (r ²)	
(r)	(r^2)	
1	1	
2	4	
3	9	
1 2 3 4 5 6 7 8	16	
5	25	
6		
7		
8		
9		
10	100	
11		
12		
13 14		
14		
15	225	
16		
17		
18		
19		
20	400	
21 22 23 24		
22		
23		
24		
25	625	
To Do		

To Do Fill in the missing Squares.